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GRADE 5 • MODULE 1

Place Value and Decimal Fractions

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NOTE: Student sheets should be printed at 100% scale to preserve the intended size of figures for accurate measurements. Adjust copier or printer settings to actual size and set page scaling to none.
Grade 5 • Module 1
Place Value and Decimal Fractions

OVERVIEW

In Module 1, students’ understandings of the patterns in the base ten system are extended from Grade 4’s work with place value to include decimals to the thousandths place. In Grade 5, students deepen their knowledge through a more generalized understanding of the relationships between and among adjacent places on the place value chart, e.g., 1 tenth times any digit on the place value chart moves the digit one place value to the right (5.NBT.1). Toward the module’s end, students apply these new understandings as they reason about and perform decimal operations through the hundredths place.

Topic A opens the module with a conceptual exploration of the multiplicative patterns of the base ten system using place value disks and a place value chart. Students notice that multiplying by 1,000 is the same as multiplying by $10 \times 10 \times 10$. Since each factor of 10 shifts the digits one place to the left, multiplying by $10 \times 10 \times 10$—which can be recorded in exponential form as $10^3$ (5.NBT.2)—shifts the position of the digits to the left 3 places, thus changing the digits’ relationships to the decimal point (5.NBT.2). Application of these place value understandings to problem solving with metric conversions completes Topic A (5.MD.1).

Topic B moves into the naming of decimal fraction numbers in expanded, unit (e.g., 4.23 = 4 ones 2 tenths 3 hundredths), and word forms and concludes with using like units to compare decimal fractions. Now in Grade 5, students use exponents and the unit fraction to represent expanded form, e.g., $2 \times 10^2 + 3 \times (1/10) + 4 \times (1/100) = 200.34$ (5.NBT.3). Further, students reason about differences in the values of like place value units and express those comparisons with symbols (>, <, and =). Students generalize their knowledge of rounding whole numbers to round decimal numbers in Topic C, initially using a vertical number line to interpret the result as an approximation and then eventually moving away from the visual model (5.NBT.4).

In the latter topics of Module 1, students use the relationships of adjacent units and generalize whole number algorithms to decimal fraction operations (5.NBT.7). Topic D uses unit form to connect general methods for addition and subtraction with whole numbers to decimal addition and subtraction, e.g., 7 tens + 8 tens = 15 tens = 150 is analogous to 7 tenths + 8 tenths = 15 tenths = 1.5.

Topic E bridges the gap between Grade 4 work with multiplication and the standard algorithm by focusing on an intermediate step—reasoning about multiplying a decimal by a one-digit whole number. The area model, with which students have had extensive experience since Grade 3, is used as a scaffold for this work.

Topic F concludes Module 1 with a similar exploration of division of decimal numbers by one-digit whole number divisors. Students solidify their skills with an understanding of the algorithm before moving on to long division involving two-digit divisors in Module 2.

The Mid-Module Assessment follows Topic C. The End-of-Module Assessment follows Topic F.
Focus Grade Level Standards

Understand the place value system.

5.NBT.1 Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and 1/10 of what it represents in the place to its left.

5.NBT.2 Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10.

5.NBT.3 Read, write, and compare decimals to thousandths.
   a. Read and write decimals to thousandths using base-ten numerals, number names, and expanded form, e.g., 347.392 = 3 × 100 + 4 × 10 + 7 × 1 + 3 × (1/10) + 9 × (1/100) + 2 × (1/1000).
   b. Compare two decimals to thousandths based on meanings of the digits in each place, using >, =, and < symbols to record the results of comparisons.

5.NBT.4 Use place value understanding to round decimals to any place.
Perform operations with multi-digit whole numbers and with decimals to hundredths.\(^1\)

**5.NBT.7** Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Convert like measurement units within a given measurement system.

**5.MD.1** Convert among different-sized standard measurement units within a given measurement system (e.g., convert 5 cm to 0.05 m), and use these conversions in solving multi-step, real world problems.\(^2\)

**Foundational Standards**

**4.NBT.1** Recognize that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right. *For example, recognize that 700 ÷ 70 = 10 by applying concepts of place value and division.*

**4.NBT.3** Use place value understanding to round multi-digit whole numbers to any place.

**4.NF.5** Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100. (Students who can generate equivalent fractions can develop strategies for adding fractions with unlike denominators in general. But addition and subtraction with unlike denominators in general is not a requirement at this grade.) *For example, express 3/10 as 30/100, and add 3/10 + 4/100 = 34/100.*

**4.NF.6** Use decimal notation for fractions with denominators 10 or 100. *For example, rewrite 0.62 as 62/100; describe a length as 0.62 meters; locate 0.62 on a number line diagram.*

**4.NF.7** Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole. Record the results of comparisons with the symbols >, =, or <, and justify the conclusions, e.g., by using a visual model.

**4.MD.1** Know relative sizes of measurement units within one system of units including km, m, cm; kg, g; lb, oz.; l, ml; hr, min, sec. Within a single system of measurement, express measurements in a larger unit in terms of a smaller unit. Record measurement equivalents in a two-column table. *For example, know that 1 ft is 12 times as long as 1 in. Express the length of a 4 ft snake as 48 in. Generate a conversion table for feet and inches listing the number pairs (1, 12), (2, 24), (3, 36), ...*

**4.MD.2** Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or \(^1\) The balance of this cluster is addressed in Module 2.

\(^2\) The focus in this module is on the metric system to reinforce place value and writing measurements using mixed units. This standard is addressed again in later modules.
decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale.

Focus Standards for Mathematical Practice

**MP.6** *Attend to precision.* Students express the units of the base ten system as they work with decimal operations, expressing decompositions and compositions with understanding, e.g., “9 hundredths + 4 hundredths = 13 hundredths. I can change 10 hundredths to make 1 tenth.”

**MP.7** *Look for and make use of structure.* Students explore the multiplicative patterns of the base ten system when they use place value charts and disks to highlight the relationships between adjacent places. Students also use patterns to name decimal fraction numbers in expanded, unit, and word forms.

**MP.8** *Look for and express regularity in repeated reasoning.* Students express regularity in repeated reasoning when they look for and use whole number general methods to add and subtract decimals and when they multiply and divide decimals by whole numbers. Students also use powers of ten to explain patterns in the placement of the decimal point and generalize their knowledge of rounding whole numbers to round decimal numbers.

Overview of Module Topics and Lesson Objectives

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<td>Lesson 1: Reason concretely and pictorially using place value understanding to relate adjacent base ten units from millions to thousandths.</td>
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<td>Lesson 2: Reason abstractly using place value understanding to relate adjacent base ten units from millions to thousandths.</td>
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<td>Lesson 3: Use exponents to name place value units and explain patterns in the placement of the decimal point.</td>
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<td>Lesson 4: Use exponents to denote powers of 10 with application to metric conversions.</td>
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<td>5.NBT.3</td>
<td><strong>Decimal Fractions and Place Value Patterns</strong></td>
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<td>Lesson 5: Name decimal fractions in expanded, unit, and word forms by applying place value reasoning.</td>
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<td>Lesson 6: Compare decimal fractions to the thousandths using like units, and express comparisons with &gt;, &lt;, =.</td>
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<td>5.NBT.4</td>
<td><strong>Place Value and Rounding Decimal Fractions</strong></td>
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<td>Lessons 7–8: Round a given decimal to any place using place value understanding and the vertical number line.</td>
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## Module Overview

### Mid-Module Assessment: Topics A–C (assessment ½ day, return ½ day, remediation or further applications 1 day)

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<td>5.NBT.7</td>
<td>Lesson 10: Subtract decimals using place value strategies and relate those strategies to a written method.</td>
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<tr>
<td>5.NBT.3</td>
<td>Lesson 11: Multiply a decimal fraction by single-digit whole numbers, relate to a written method through application of the area model and place value understanding, and explain the reasoning used.</td>
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<tr>
<td>5.NBT.7</td>
<td>Lesson 12: Multiply a decimal fraction by single-digit whole numbers, including using estimation to confirm the placement of the decimal point.</td>
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<td>5.NBT.3</td>
<td>Dividing Decimals</td>
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<td>5.NBT.7</td>
<td>Lesson 13: Divide decimals by single-digit whole numbers involving easily identifiable multiples using place value understanding and relate to a written method.</td>
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<td>Lesson 14: Divide decimals with a remainder using place value understanding and relate to a written method.</td>
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<td>Lesson 15: Divide decimals using place value understanding including remainders in the smallest unit.</td>
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<td>Lesson 16: Solve word problems using decimal operations.</td>
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### Total Number of Instructional Days

- **20**
Module Overview

Terminology

New or Recently Introduced Terms

- Exponent (how many times a number is to be used in a multiplication sentence)
- Millimeter (a metric unit of length equal to one-thousandth of a meter)
- Thousandths (related to place value)

Familiar Terms and Symbols

- $>, <, =$ (greater than, less than, equal to)
- Base ten units (place value units)
- Bundling, making, renaming, changing, regrouping, trading
- Centimeter (cm, a unit of measure equal to one-hundredth of a meter)
- Digit (any of the numbers 0 to 9; e.g., what is the value of the digit in the tens place?)
- Expanded form (e.g., 135 = 1 × 100 + 3 × 10 + 5 × 1)
- Hundredths (as related to place value)
- Number line (a line marked with numbers at evenly spaced intervals)
- Number sentence (e.g., $4 + 3 = 7$)
- Place value (the numerical value that a digit has by virtue of its position in a number)
- Standard form (a number written in the format: 135)
- Tenths (as related to place value)
- Unbundling, breaking, renaming, changing, regrouping, trading
- Unit form (e.g., 3.21 = 3 ones 2 tenths 1 hundredth)
- Word form (e.g., one hundred thirty-five)

Suggested Tools and Representations

- Number lines (a variety of templates, including a large one for the back wall of the classroom)
- Place value charts (at least one per student for an insert in their personal board)
- Place value disks

NOTES ON EXPRESSION, EQUATION, AND NUMBER SENTENCE:

Please note the descriptions for the following terms, which are frequently misused.

- **Expression**: A number, or any combination of sums, differences, products, or divisions of numbers that evaluates to a number (e.g., $3 + 4, 8 \times 3, 15 \div 3$ as distinct from an equation or number sentence).
- **Equation**: A statement that two expressions are equal (e.g., $3 \times ___ = 12, 5 \times b = 20, 3 + 2 = 5$).
- **Number sentence** (also addition, subtraction, multiplication, or division sentence): An equation or inequality for which both expressions are numerical and can be evaluated to a single number (e.g., $4 + 3 = 6 + 1, 2 = 2, 21 > 7 \times 2, 5 + 5 = 10$). Number sentences are either true or false (e.g., $4 + 4 < 6 \times 2$ and $21 \div 7 = 4$) and contain no unknowns.

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3 These are terms and symbols students have used or seen previously.
Suggested Methods of Instructional Delivery

Directions for Administration of Sprints

Sprints are designed to develop fluency. They should be fun, adrenaline-rich activities that intentionally build energy and excitement. A fast pace is essential. During Sprint administration, teachers assume the role of athletic coaches. A rousing routine fuels students’ motivation to do their personal best. Student recognition of increasing success is critical, and so every improvement is celebrated.

One Sprint has two parts with closely related problems on each. Students complete the two parts of the Sprint in quick succession with the goal of improving on the second part, even if only by one more.

With practice, the following routine takes about 9 minutes.

Sprint A

Pass Sprint A out quickly, face down on student desks with instructions to not look at the problems until the signal is given. (Some Sprints include words. If necessary, prior to starting the Sprint, quickly review the words so that reading difficulty does not slow students down.)

T:  You will have 60 seconds to do as many problems as you can. I do not expect you to finish all of them. Just do as many as you can, your personal best. (If some students are likely to finish before time is up, assign a number to count by on the back.)

T:  Take your mark! Get set! THINK!

Students immediately turn papers over and work furiously to finish as many problems as they can in 60 seconds. Time precisely.

T:  Stop! Circle the last problem you did. I will read just the answers. If you got it right, call out “Yes!” If you made a mistake, circle it. Ready?

T:  (Energetically, rapid-fire call the first answer.)
S:  Yes!
T:  (Energetically, rapid-fire call the second answer.)
S:  Yes!

Repeat to the end of Sprint A or until no student has a correct answer. If needed, read the count-by answers in the same way you read Sprint answers. Each number counted-by on the back is considered a correct answer.

T:  Fantastic! Now, write the number you got correct at the top of your page. This is your personal goal for Sprint B.

T:  How many of you got one right? (All hands should go up.)

T:  Keep your hand up until I say the number that is one more than the number you got correct. So, if you got 14 correct, when I say 15, your hand goes down. Ready?

T:  (Continue quickly.) How many got two correct? Three? Four? Five? (Continue until all hands are down.)

If the class needs more practice with Sprint A, continue with the optional routine presented below.
T: I'll give you one minute to do more problems on this half of the Sprint. If you finish, stand behind your chair.

As students work, the student who scored highest on Sprint A might pass out Sprint B.

T: Stop! I will read just the answers. If you got it right, call out “Yes!” If you made a mistake, circle it. Ready? (Read the answers to the first half again as students stand.)

Movement

To keep the energy and fun going, always do a stretch or a movement game in between Sprints A and B. For example, the class might do jumping jacks while skip-counting by 5 for about 1 minute. Feeling invigorated, students take their seats for Sprint B, ready to make every effort to complete more problems this time.

Sprint B

Pass Sprint B out quickly, face down on student desks with instructions to not look at the problems until the signal is given. (Repeat the procedure for Sprint A up through the show of hands for how many right.)

T: Stand up if you got more correct on the second Sprint than on the first.
S: (Stand.)
T: Keep standing until I say the number that tells how many more you got right on Sprint B. If you got three more right on Sprint B than you did on Sprint A, when I say three, you sit down. Ready? (Call out numbers starting with one. Students sit as the number by which they improved is called. Celebrate the students who improved most with a cheer.)

T: Well done! Now, take a moment to go back and correct your mistakes. Think about what patterns you noticed in today’s Sprint.

T: How did the patterns help you get better at solving the problems?

T: Rally Robin your thinking with your partner for 1 minute. Go!

Rally Robin is a style of sharing in which partners trade information back and forth, one statement at a time per person, for about 1 minute. This is an especially valuable part of the routine for students who benefit from their friends’ support to identify patterns and try new strategies.

Students may take Sprints home.

RDW or Read, Draw, Write (an Equation and a Statement)

Mathematicians and teachers suggest a simple process applicable to all grades:

1) Read.
2) Draw and Label.
3) Write an equation.
4) Write a word sentence (statement).

The more students participate in reasoning through problems with a systematic approach, the more they internalize those behaviors and thought processes.

- What do I see?
- Can I draw something?
- What conclusions can I make from my drawing?

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<th>Modeling with Interactive Questioning</th>
<th>Guided Practice</th>
<th>Independent Practice</th>
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<tr>
<td>The teacher models the whole process with interactive questioning, some choral response, and talk moves such as, “What did Monique say, everyone?” After completing the problem, students might reflect with a partner on the steps they used to solve the problem. “Students, think back on what we did to solve this problem. What did we do first?” Students might then be given the same or similar problem to solve for homework.</td>
<td>Each student has a copy of the question. Though guided by the teacher, they work independently at times and then come together again. Timing is important. Students might hear, “You have 2 minutes to do your drawing.” Or, “Put your pencils down. Time to work together again.” The Debrief might include selecting different student work to share.</td>
<td>The students are given a problem to solve and possibly a designated amount of time to solve it. The teacher circulates, supports, and is thinking about which student work to show to support the mathematical objectives of the lesson. When sharing student work, students are encouraged to think about the work with questions such as, “What do you notice about Jeremy’s work?”, “What is the same about Jeremy’s work and Sara’s work?”, “How did Jeremy show the 3/7 of the students?”, and “How did Sara show the 3/7 of the students?”</td>
</tr>
</tbody>
</table>

Personal White Boards

Materials Needed for Personal White Boards

1 heavy duty clear sheet protector
1 piece of stiff red tag board 11" × 8 ¼"
1 piece of stiff white tag board 11" × 8 ¼"
1 3" × 3" piece of dark synthetic cloth for an eraser (e.g., felt)
1 low odor blue dry erase marker, fine point

Directions for Creating Personal White Boards

Cut your white and red tag to specifications. Slide into the sheet protector. Store your eraser on the red side. Store markers in a separate container to avoid stretching the sheet protector.

Frequently Asked Questions About Personal White Boards

Why is one side red and one white?

The white side of the board is the “paper.” Students generally write on it, and if working individually, turn the board over to signal to the teacher they have completed their work. The teacher then says,
“Show me your boards,” when most of the class is ready.

What are some of the benefits of a personal white board?

- The teacher can respond quickly to a gap in student understandings and skills. “Let’s do some of these on our personal white boards until we have more mastery.”
- Students can erase quickly so that they do not have to suffer the evidence of their mistake.
- They are motivating. Students love both the drill and thrill capability and the chance to do story problems with an engaging medium.
- Checking work gives the teacher instant feedback about student understanding.

What is the benefit of this personal white board over a commercially purchased dry erase board?

- It is much less expensive.
- Templates such as place value charts, number bond mats, hundreds boards, and number lines can be stored between the two pieces of tag board for easy access and reuse.
- Worksheets, story problems, and other problem sets can be done without marking the paper so that students can work on the problems independently at another time.
- Strips with story problems, number lines, and arrays can be inserted and still have a full piece of paper on which to write.
- The red versus white side distinction clarifies your expectations. When working collaboratively, there is no need to use the red. When working independently, the students know how to keep their work private.
- The tag board can be removed so that student work can be projected on an overhead.

Scaffolds

The scaffolds integrated into A Story of Units give alternatives for how students access information as well as express and demonstrate their learning. Strategically placed margin notes are provided within each lesson, elaborating on the use of specific scaffolds at applicable times. They address many needs presented by English language learners, students with disabilities, students performing above grade level, and students performing below grade level. Many of the suggestions are organized by Universal Design for Learning (UDL) principles and are applicable to more than one population. To read more about the approach to differentiated instruction in A Story of Units, please refer to “How to Implement A Story of Units.”

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4 Students with disabilities may require Braille, large print, audio, or special digital files. Please visit the website, www.p12.nysed.gov/specialed/aim, for specific information on how to obtain student materials that satisfy the National Instructional Materials Accessibility Standard (NIMAS) format.
### Assessment Summary

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<td>After Topic C</td>
<td>Constructed response with rubric</td>
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<td>End-of-Module Assessment Task</td>
<td>After Topic F</td>
<td>Constructed response with rubric</td>
<td>5.NBT.1 5.NBT.2 5.NBT.3 5.NBT.4 5.NBT.7 5.MD.1</td>
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Lesson 1

Objective: Reason concretely and pictorially using place value understanding to relate adjacent base ten units from millions to thousandths.

Suggested Lesson Structure

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<th>Component</th>
<th>Time</th>
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<td>Fluency Practice</td>
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<tr>
<td>Application Problem</td>
<td>8 min</td>
</tr>
<tr>
<td>Concept Development</td>
<td>30 min</td>
</tr>
<tr>
<td>Student Debrief</td>
<td>10 min</td>
</tr>
<tr>
<td>Total Time</td>
<td>60 min</td>
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Fluency Practice (12 minutes)

- Sprint: Multiply by 10 4.NBT.1 (8 minutes)
- Rename the Units 2.NBT.1 (2 minutes)
- Decimal Place Value 4.NF.5–6 (2 minutes)

Sprint: Multiply by 10 (8 minutes)

Materials: (S) Multiply by 10 Sprint

Note: Reviewing this fluency activity will acclimate students to the Sprint routine, a vital component of the fluency program.

Please see Directions for Administration of Sprints in the Module Overview for tips on implementation.

Rename the Units—Choral Response (2 minutes)

Notes: This fluency activity reviews foundations that lead into today’s lesson.

  T:  (Write 10 ones = _____ ten.) Say the number sentence.
  S:  10 ones = 1 ten.
  T:  (Write 20 ones = _____ tens.) Say the number sentence.
  S:  20 ones = 2 tens.
  T:  30 ones.
Lesson 1

S: 3 tens.
Repeat the process for 80 ones, 90 ones, 100 ones, 110 ones, 120 ones, 170, 270, 670, 640, and 830.

**Decimal Place Value (2 minutes)**

Materials: (S) Personal white board, unlabeled hundreds to hundredths place value chart (Template 1)

Note: Reviewing this Grade 4 topic lays a foundation for students to better understand place value to bigger and smaller units.

T: (Project unlabeled hundreds to hundredths place value chart. Draw 3 ten disks in the tens column.) How many tens do you see?
S: 3 tens.
T: (Write 3 underneath the disks.) There are 3 tens and how many ones?
S: Zero ones.
T: (Write 0 in the ones column. Below it, write 3 tens = ___.) Fill in the blank.
S: 3 tens = 30.
Repeat the process for 3 tenths = 0.3.
T: (Write 4 tenths = ___.) Show the answer in your place value chart.
S: (Draw four 1 tenth disks. Below it, write 0.4.)

Repeat the process for 3 hundredths, 43 hundredths, 5 hundredths, 35 hundredths, 7 ones 35 hundredths, 9 ones 24 hundredths, and 6 tens 2 ones 4 hundredths.

Note: Place value disks are used as models throughout the curriculum and can be represented in two different ways. A disk with a value labeled inside of it (above) should be drawn or placed on a place value chart with no headings. The value of the disk in its appropriate column indicates the column heading. A place value disk drawn as a dot should be used on place value charts with headings, as shown in Problem 1 of Concept Development. The dot is a faster way to represent the place value disk and is used as students move further away from a concrete stage of learning.

Application Problem (8 minutes)

Farmer Jim keeps 12 hens in every coop. If Farmer Jim has 20 coops, how many hens does he have in all? If every hen lays 9 eggs on Monday, how many eggs will Farmer Jim collect on Monday? Explain your reasoning using words, numbers, or pictures.

Note: This problem is intended to activate prior knowledge from Grade 4 and offer a successful start to Grade 5. Some students may use area models to solve, while others may choose to use the standard algorithm. Still others may draw tape diagrams to show their thinking. Allow students to share work and compare approaches.
Concept Development (30 minutes)

Materials: (S) Millions through thousandths place value chart (Template 2), personal white board

The place value chart and its \(times 10\) relationships are familiar territory for students. New learning in Grade 5 focuses on understanding a new fractional unit of thousandths as well as the decomposition of larger units to those that are 1 tenth as large. Building the place value chart from right (tenths) to left (millions) before beginning the following problem sequence may be advisable. Encourage students to multiply and then bundle to form next largest place (e.g., \(10 \times 1\) hundred = 10 hundreds, which can be bundled to form 1 thousand).

Problem 1: Divide single units by 10 to build the place value chart to introduce thousandths.

T: Slide your millions through thousandths place value chart into your personal white board. Show 1 million, using disks, on place value chart.

S: (Work.)

T: How can we show 1 million using hundred thousands? Work with your partner to show this on your chart.

S: 1 million is the same as 10 hundred thousands.

T: What is the result if I divide 10 hundred thousands by 10? Talk with your partner and use your chart to find the quotient.

T: (Circulate.) I saw that David put 10 disks in the hundred thousands place and then distributed them into 10 equal groups. How many are in each group?

S: When I divide 10 hundred thousands by 10, I get 1 hundred thousand in each group.

T: Let me record what I hear you saying. (Record on class board.)

\[
10 \text{ hundred thousands} \div 10 = 1 \text{ hundred thousand} \\
1 \text{ million} \div 10 = 1 \text{ hundred thousand}
\]

1 hundred thousand is \(\frac{1}{10}\) as large as 1 million.

T: Draw 1 hundred thousand disk on your chart. What is the result if we divide 1 hundred thousand by 10? Show this on your chart and write a division sentence.
Lesson 1:

Reason concretely and pictorially using place value understanding to relate adjacent base ten units from millions to thousandths.

1. A. 6

NOTES ON MULTIPLE MEANS OF ENGAGEMENT:

Students who have limited experience with decimal fractions may be supported by a return to Grade 4’s Module 6 to review decimal place value and symmetry with respect to the ones place. Conversely, student understanding of decimal fraction place value units may be extended by asking for predictions of units one-tenth as large as the thousandths place and those beyond.

NOTES ON MULTIPLE MEANS OF ENGAGEMENT:

Proportional materials such as base ten blocks can help English language learners distinguish between place value labels like hundredth and thousandth more easily by offering clues to their relative sizes. These students can be encouraged to name the units in their first language and then compare them to their English counterparts. Sometimes the roots of these number words are very similar. These parallels enrich the experience and understanding of all students.

Continue this sequence until the hundredths place is reached, emphasizing the unbundling for 10 of the smaller unit and then the division. Record the place values and equations (using unit form) on the board being careful to point out the 1 tenth as large relationship:

1 million ÷ 10 = 1 hundred thousand
1 hundred thousand ÷ 10 = 1 ten thousand
1 ten thousand ÷ 10 = 1 thousand
1 thousand ÷ 10 = 1 hundred

(Continue through 1 tenth ÷ 10 = 1 hundredth.)

T: What patterns do you notice in the way the units are named in our place value system?
S: The ones place is the middle. There are tens on the left and tenths on the right, hundreds on the left and hundredths on the right.

T: (Point to the chart.) Using this pattern, can you predict what the name of the unit that is to the right of the hundredths place (1 tenth as large as hundredths) might be?
S: (Share. Label the thousandths place.)

T: Think about the pattern that we’ve seen with other adjacent places. Talk with your partner and predict how we might show 1 hundredth using thousandths disks. Show this on your chart.
S: Just like all the other places, it takes 10 of the smaller unit to make 1 of the larger, so it will take 10 thousandths to make 1 hundredth.

T: Use your chart to show the result if we divide 1 hundredth by 10, and write the division sentence.
S: (Share.)
T: (Add this equation to the others on the board.)

Problem 2: Multiply copies of one unit by 10, 100, and 1,000.

0.4 × 10
0.04 × 10
0.004 × 10

T: Use digits to represent 4 tenths at the top of your place value chart.
S: (Write.)
T: Work with your partner to find the value of 10 times 0.4. Show your result at the bottom of your place value chart.

S: 4 tenths × 10 = 40 tenths, which is the same as 4 wholes. → 4 ones is 10 times as large as 4 tenths.

T: On your place value chart, use arrows to show how the value of the digits has changed. (On place value chart, draw an arrow to indicate the shift of the digit to the left, write × 10 near the arrow.)

T: Why does the digit move one place to the left?

S: Because it is 10 times as large, it has to be bundled for the next larger unit.

Repeat with 0.04 × 10 and 0.004 × 1,000. Use unit form to state each problem, and encourage students to articulate how the value of the digit changes and why it changes position in the chart.

**Problem 3:** Divide copies of one unit by 10, 100, and 1,000.

6 ÷ 10
6 ÷ 100
6 ÷ 1,000

Follow a similar sequence to guide students in articulating changes in value and shifts in position while showing it on the place value chart.

Repeat with 0.7 ÷ 10, 0.7 ÷ 100, and 0.05 ÷ 10.

**Problem 4:** Multiply mixed units by 10, 100, and 1,000.

2.43 × 10
2.43 × 100
2.43 × 1,000

T: Write the digits two and forty-three hundredths on your place value chart, and multiply by 10, then 100, and then 1,000. Compare these products with your partner.

Lead students to discuss how the digits shift as a result of their change in value by isolating one digit, such as the 3, and comparing its value in each product.

**Problem 5**

745 ÷ 10
745 ÷ 100
745 ÷ 1,000

Engage in a similar discussion regarding the shift and change in value for a digit in these division problems. See discussion above.
Problem Set (10 minutes)

Students should do their personal best to complete the Problem Set within the allotted 10 minutes. Some problems do not specify a method for solving. This is an intentional reduction of scaffolding that invokes MP.5, Use Appropriate Tools Strategically. Students should solve these problems using the RDW approach used for Application Problems.

For some classes, it may be appropriate to modify the assignment by specifying which problems students should work on first. With this option, let the purposeful sequencing of the problem set guide your selections so that problems continue to be scaffolded. Balance word problems with other problem types to ensure a range of practice. Consider assigning incomplete problems for homework or at another time during the day.

Student Debrief (10 minutes)

Lesson Objective: Reason concretely and pictorially using place value understanding to relate adjacent base ten units from millions to thousandths.

The Student Debrief is intended to invite reflection and active processing of the total lesson experience.

Invite students to review their solutions for the Problem Set. They should check work by comparing answers with a partner before going over answers as a class. Look for misconceptions or misunderstandings that can be addressed in the Debrief. Guide students in a conversation to debrief the Problem Set and process the lesson.

You may choose to use any combination of the questions below to lead the discussion.

- Compare the solutions you found when multiplying by 10 and dividing by 10 \((3.452 \times 10\) and \(345 \div 10\)). How do the solutions of these two expressions relate to the value of the original quantity? How do they relate to each other?
- What do you notice about the number of zeros in your products when multiplying by 10, 100, and 1,000 relative to the number of places the digits shift on the place value chart? What patterns do you notice?
Lesson 1:

- What is the same and what is different about the products for Problems 1(a), 1(b), and 1(c)? (Encourage students to notice that the digits are exactly the same. Only the values have changed.)
- When solving Problem 2(c), many of you noticed the use of our new place value. (Lead brief class discussion to reinforce what value this place represents. Reiterate the symmetry of the places on either side of the ones place and the size of thousandths relative to other place values like tenths and ones.)

Exit Ticket (3 minutes)

After the Student Debrief, instruct students to complete the Exit Ticket. A review of their work will help you assess the students’ understanding of the concepts that were presented in the lesson today and plan more effectively for future lessons. You may read the questions aloud to the students.
Lesson 1 Sprint

Lesson 1: Reason concretely and pictorially using place value understanding to relate adjacent base ten units from millions to thousandths.

Date: 10/21/14

<table>
<thead>
<tr>
<th></th>
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<th># Correct _____</th>
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<tbody>
<tr>
<td>1</td>
<td>12 x 10 =</td>
<td>23</td>
</tr>
<tr>
<td>2</td>
<td>14 x 10 =</td>
<td>24</td>
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<td>3</td>
<td>15 x 10 =</td>
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<td>4</td>
<td>17 x 10 =</td>
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<td>5</td>
<td>81 x 10 =</td>
<td>27</td>
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<td>6</td>
<td>10 x 81 =</td>
<td>28</td>
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<tr>
<td>7</td>
<td>21 x 10 =</td>
<td>29</td>
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<tr>
<td>8</td>
<td>22 x 10 =</td>
<td>30</td>
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<tr>
<td>9</td>
<td>23 x 10 =</td>
<td>31</td>
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<tr>
<td>10</td>
<td>29 x 10 =</td>
<td>32</td>
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<tr>
<td>11</td>
<td>92 x 10 =</td>
<td>33</td>
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<tr>
<td>12</td>
<td>10 x 92 =</td>
<td>34</td>
</tr>
<tr>
<td>13</td>
<td>18 x 10 =</td>
<td>35</td>
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<tr>
<td>14</td>
<td>19 x 10 =</td>
<td>36</td>
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<tr>
<td>15</td>
<td>20 x 10 =</td>
<td>37</td>
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<tr>
<td>16</td>
<td>30 x 10 =</td>
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<tr>
<td>17</td>
<td>40 x 10 =</td>
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<tr>
<td>18</td>
<td>80 x 10 =</td>
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<tr>
<td>19</td>
<td>10 x 80 =</td>
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<td>20</td>
<td>10 x 50 =</td>
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<tr>
<td>21</td>
<td>10 x 90 =</td>
<td>43</td>
</tr>
<tr>
<td>22</td>
<td>10 x 70 =</td>
<td>44</td>
</tr>
</tbody>
</table>
## Lesson 1 Sprint

**Lesson 1:**
Reason concretely and pictorially using place value understanding to relate adjacent base ten units from millions to thousandths.

**Date:** 10/21/14

<table>
<thead>
<tr>
<th>Improvement</th>
<th># Correct</th>
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<tbody>
<tr>
<td><strong>Multiply.</strong></td>
<td></td>
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<tr>
<td>13 x 10 =</td>
<td>23 43 x 10 =</td>
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<tr>
<td>14 x 10 =</td>
<td>24 143 x 10 =</td>
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<td>15 x 10 =</td>
<td>25 243 x 10 =</td>
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<td>19 x 10 =</td>
<td>26 343 x 10 =</td>
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<td>91 x 10 =</td>
<td>27 743 x 10 =</td>
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<td>10 x 91 =</td>
<td>28 10 x 743 =</td>
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<td>31 x 10 =</td>
<td>29 54 x 10 =</td>
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<td>32 x 10 =</td>
<td>30 154 x 10 =</td>
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<td>33 x 10 =</td>
<td>31 254 x 10 =</td>
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<td>38 x 10 =</td>
<td>32 354 x 10 =</td>
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<tr>
<td>83 x 10 =</td>
<td>33 854 x 10 =</td>
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<td>10 x 83 =</td>
<td>34 65 x 10 =</td>
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<td>28 x 10 =</td>
<td>35 465 x 10 =</td>
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<td>29 x 10 =</td>
<td>36 565 x 10 =</td>
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<td>30 x 10 =</td>
<td>37 960 x 10 =</td>
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<td>40 x 10 =</td>
<td>38 10 x 960 =</td>
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<tr>
<td>50 x 10 =</td>
<td>39 17 x 10 =</td>
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<tr>
<td>90 x 10 =</td>
<td>40 10 x 70 =</td>
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<tr>
<td>10 x 90 =</td>
<td>41 582 x 10 =</td>
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<tr>
<td>10 x 20 =</td>
<td>42 10 x 73 =</td>
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<tr>
<td>10 x 60 =</td>
<td>43 98 x 10 =</td>
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<tr>
<td>10 x 80 =</td>
<td>44 10 x 470 =</td>
</tr>
</tbody>
</table>
1. Use the place value chart and arrows to show how the value of each digit changes. The first one has been done for you.

   a. $3.452 \times 10 = 34.52$

   b. $3.452 \times 100 = ______$

   c. $3.452 \times 1,000 = ______$

   d. Explain how and why the value of the 5 changed in (a), (b), and (c).
2. Use the place value chart and arrows to show how the value of each digit changes. The first one has been done for you.

   a. \(345 \div 10 = 34.5\)

   b. \(345 \div 100 = \) ______

   c. \(345 \div 1,000 = \) ______

   d. Explain how and why the value of the 4 changed in the quotients in (a), (b), and (c).
3. A manufacturer made 7,234 boxes of coffee stirrers. Each box contains 1,000 stirrers. How many stirrers did they make? Explain your thinking, and include a statement of the solution.

4. A student used his place value chart to show a number. After the teacher instructed him to multiply his number by 10, the chart showed 3,200.4. Draw a picture of what the place value chart looked like at first.

<table>
<thead>
<tr>
<th></th>
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</tbody>
</table>

a. Explain how you decided what to draw on your place value chart. Be sure to include your reasoning about how the value of each digit was affected by the multiplication. Use words, pictures, or numbers.

5. A microscope has a setting that magnifies an object so that it appears 100 times as large when viewed through the eyepiece. If a tiny insect is 0.095 cm long, how long will the insect appear in centimeters through the microscope? Explain how you know.
1. Use the place value chart and arrows to show how the value of each digit changes.

   a. \(6.671 \times 100 = \) __________

   b. \(684 \div 1,000 = \) __________
1. Use the place value chart and arrows to show how the value of each digit changes. The first one has been done for you.

   a. \(4.582 \times 10 = 45.82\)

   b. \(7.281 \times 100 = \underline{728.1}\)

   c. \(9.254 \times 1,000 = \underline{9254}\)

   d. Explain how and why the value of the 2 changed in (a), (b), and (c).
2. Use the place value chart and arrows to show how the value of each digit changes. The first one has been done for you.

a. \[2.46 \div 10 = 0.246\]

b. \[678 \div 100 = \_\_\_\_\_

\[\begin{array}{c|c|c}
\hline
& 2 & 4 6 \\
\hline
\end{array}
\]

\[\begin{array}{c|c|c}
\hline
& 6 & 7 8 \\
\hline
\end{array}
\]

c. \[67 \div 1,000 = \_\_\_\_\_

\[\begin{array}{c|c|c}
\hline
& 2 & 4 6 \\
\hline
\end{array}
\]

\[\begin{array}{c|c|c}
\hline
& 6 7 & \\
\hline
\end{array}
\]

d. Explain how and why the value of the 6 changed in the quotients in (a), (b), and (c).
3. Researchers counted 8,912 monarch butterflies on one branch of a tree at a site in Mexico. They estimated that the total number of butterflies at the site was 1,000 times as large. About how many butterflies were at the site in all? Explain your thinking, and include a statement of the solution.

4. A student used his place value chart to show a number. After the teacher instructed him to divide his number by 100, the chart showed 28.003. Draw a picture of what the place value chart looked like at first.

| 2 | 8 | 0 | 0 | 3 |

a. Explain how you decided what to draw on your place value chart. Be sure to include your reasoning about how the value of each digit was affected by the division.

5. On a map, the perimeter of a park is 0.251 meters. The actual perimeter of the park is 1,000 times as large. What is the actual perimeter of the park? Explain how you know using a place value chart.
Lesson 1: Reason concretely and pictorially using place value understanding to relate adjacent base ten units from millions to thousandths.

Date: 10/21/14

unlabeled hundreds through hundredths place value chart
Lesson 1: Reason concretely and pictorially using place value understanding to relate adjacent base ten units from millions to thousandths.

Date: 10/21/14

<table>
<thead>
<tr>
<th>Millions</th>
<th>Hundred Thousands</th>
<th>Ten Thousands</th>
<th>Thousands</th>
<th>Hundreds</th>
<th>Tens</th>
<th>Ones</th>
<th>( \frac{1}{10} )</th>
<th>( \frac{1}{100} )</th>
<th>( \frac{1}{1000} )</th>
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<tr>
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<td>10,000</td>
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</tbody>
</table>

millions through thousandths place value chart
1. The following equations involve different quantities and use different operations, yet produce the same result. Use a place value chart and words to explain why this is true.

\[ 4.13 \times 10^3 = 4130 \quad 413,000 \div 10^2 = 4130 \]

2. Use an area model to explain the product of 4.6 and 3. Write the product in standard form, word form, and expanded form.
3. Compare using >, <, or =.

a. 2 tenths + 11 hundredths  \( \bigcirc \) 0.13

b. 13 tenths + 8 tenths + 32 hundredths  \( \bigcirc \) 2.42

c. 342 hundredths + 7 tenths  \( \bigcirc \) 3 + 49 hundredths

d. \( 2 + 31 \times \frac{1}{10} + 14 \times \frac{1}{100} \)  \( \bigcirc \) 2.324

e. \( 14 + 72 \times \frac{1}{10} + 4 \times \frac{1}{1000} \)  \( \bigcirc \) 21.24

f. \( 0.3 \times 10^2 + 0.007 \times 10^3 \)  \( \bigcirc \) \( 0.3 \times 10 + 0.7 \times 10^2 \)
4. Dr. Mann mixed 10.357 g of chemical A, 12.062 g of chemical B, and 7.506 g of chemical C to make 5 doses of medicine.
   a. About how much medicine did he make in grams? Estimate the amount of each chemical by rounding to the nearest tenth of a gram before finding the sum. Show all your thinking.

   b. Find the actual amount of medicine mixed by Dr. Mann. What is the difference between your estimate and the actual amount?

   c. How many grams are in one dose of medicine? Explain your strategy for solving this problem.

   d. Round the weight of one dose to the nearest gram.
End-of-Module Assessment Task Standards Addressed

Generalize place value understanding for multi-digit whole numbers.

5.NBT.1 Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and 1/10 of what it represents in the place to its left.

5.NBT.2. Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10.

5.NBT.3 Read, write, and compare decimals to thousandths.
   a. Read and write decimals to thousandths using base-ten numerals, number names, and expanded form, e.g., 347.392 = 3 × 100 + 4 × 10 + 7 × 1 + 3 × (1/10) + 9 × (1/100) + 2 × (1/1000).
   b. Compare two decimals to thousandths based on meanings of the digits in each place, using >, =, and < symbols to record the results of comparisons.

5.NBT.4 Use place value understanding to round decimals to any place.

Perform operations with multi-digit whole numbers and with decimals to hundredths.

5.NBT.7 Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Convert like measurement units within a given measurement system.

5.MD.1 Convert among different-sized standard measurement units within a given measurement system (e.g., convert 5 cm to 0.05 m), and use these conversions in solving multi-step, real world problems.

Evaluating Student Learning Outcomes

A Progression Toward Mastery is provided to describe steps that illuminate the gradually increasing understandings that students develop on their way to proficiency. In this chart, this progress is presented from left (Step 1) to right (Step 4). The learning goal for each student is to achieve Step 4 mastery. These steps are meant to help teachers and students identify and celebrate what the student CAN do now, and what they need to work on next.
<table>
<thead>
<tr>
<th>Assessment Task Item and Standards Assessed</th>
<th>STEP 1</th>
<th>STEP 2</th>
<th>STEP 3</th>
<th>STEP 4</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Little evidence of reasoning without a correct answer.</td>
<td>Evidence of some reasoning without a correct answer.</td>
<td>Evidence of some reasoning with a correct answer or evidence of solid reasoning with an incorrect answer.</td>
<td>Evidence of solid reasoning with a correct answer.</td>
</tr>
<tr>
<td></td>
<td>(1 Point)</td>
<td>(2 Points)</td>
<td>(3 Points)</td>
<td>(4 Points)</td>
</tr>
</tbody>
</table>
| 1                                         | 5.NBT.1 5.NBT.2 | The student is unable to provide a correct response. | The student attempts but is not able to accurately draw the place value chart or explain reasoning fully. | The student correctly draws place chart but does not show full reasoning, or explains reasoning fully but the place value chart does not match the reasoning. | The student correctly:  
• Draws place value chart showing movement of digits.  
• Explains movement of units to the left for multiplication and movement of units to the right for division. |
| 2                                         | 5.NBT.7 | The student is unable to use the area model to find the product. | The student attempts using an area model to multiply but does so inaccurately. Student attempts to write either word or expanded form of inaccurate product. | The student uses the area model to multiply but does not find the correct product. Student accurately produces word and expanded form of inaccurate product. | The student correctly:  
• Draws an area model.  
• Shows work to find product 13.8.  
• Accurately expresses product in both word and expanded form. |
| 3                                         | 5.NBT.3a 5.NBT.3b | The student answers none or one part correctly. | The student answers two or three answers correctly. | The student answers four or five answers correctly. | The student correctly answers all six parts.  
  a. >  
  b. =  
  c. >  
  d. >  
  e. <  
  f. < |
| 4 | 5.NBT.1  
   5.NBT.2  
   5.NBT.3a  
   5.NBT.3b  
   5.NBT.4  
   5.NBT.7  
   5.MD.1 | The student answers none or one part correctly. |
<table>
<thead>
<tr>
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<th></th>
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</thead>
<tbody>
<tr>
<td></td>
<td>The student answers two parts correctly.</td>
</tr>
<tr>
<td></td>
<td>The student is able to find all answers correctly but is unable to explain strategy in Part(c), or answers three of the four parts correctly.</td>
</tr>
<tr>
<td></td>
<td>The student correctly:</td>
</tr>
<tr>
<td></td>
<td>a. Estimates 10.357 g to 10.4 g, 12.062 g to 12.1 g, and 7.506 g as 7.5 g; finds sum 30 g; shows work or model.</td>
</tr>
<tr>
<td></td>
<td>b. Finds sum 29.925 g and difference 0.075 g.</td>
</tr>
<tr>
<td></td>
<td>c. Finds the quotient 5.985 g and explains accurately the strategy used.</td>
</tr>
<tr>
<td></td>
<td>d. Rounds 5.985 g to 6 g.</td>
</tr>
</tbody>
</table>
1. The following equations involve different quantities and use different operations, yet produce the same result. Use a place value chart and words to explain why this is true.

\[ 4.13 \times 10^3 = 4130 \]
\[ 413,000 \div 10^2 = 4130 \]

When I multiplied, the digits moved 3 places to the left, because they got larger. When I divided, the digits moved 2 places to the right, because they decreased.

2. Use an area model to explain the product of 4.6 and 3. Write the product in standard form, word form, and expanded form.

\[
\begin{array}{c|c|c}
\text{3} & \text{4 ones} & 6 \\
\text{12 ones} & 3 \times 6 & 18 \text{ tenths} \\
\hline
12 & +1.8 & = 13.8 \\
\end{array}
\]

thirteen and eight tenths

\[ 1 \times 10 + 3 \times 1 + 8 \times \frac{1}{10} \]
3. Compare using >, <, or =.

a. 2 tenths + 11 hundredths \( \text{>} \) 0.13

b. 13 tenths + 8 tenths + 32 hundredths \( = \) 2.42

c. 342 hundredths + 7 tenths \( \text{>} \) 3 + 49 hundredths

d. \( 2 + 31 \times \frac{1}{10} + 14 \times \frac{1}{100} \) \( \text{>} \) 2.324

e. \( 14 + 72 \times \frac{1}{10} + 4 \times \frac{1}{1000} \) \( \text{<} \) 21.24

f. \( 0.3 \times 10^2 + 0.007 \times 10^3 \) \( \text{<} \) \( 0.3 \times 10 + 0.7 \times 10^2 \)
4. Dr. Mann mixed 10.357 g of chemical A, 12.062 g of chemical B, and 7.506 g of chemical C to make 5 doses of medicine.
   a. About how much medicine did he make in grams? Estimate the amount of each chemical by rounding to the nearest tenth of a gram before finding the sum. Show all your thinking.

   \[
   \begin{array}{c|c|c}
   A & 10.357 g & 10.4 g \\
   B & 12.062 g & 12.1 g \\
   C & 7.506 g & 7.5 g \\
   \hline
   & 30.0 & Dr. Mann made about 30 grams of medicine.
   \end{array}
   \]

   b. Find the actual amount of medicine mixed by Dr. Mann. What is the difference between your estimate and the actual amount?

   \[
   \begin{array}{c}
   10.357 \\
   12.062 \\
   + 7.506
   \end{array}
   \]

   \[
   \begin{array}{c}
   29.925 \\
   \hline
   29.925
   \end{array}
   \]

   \[
   \begin{array}{c}
   29.925 \\
   - 29.925 \\
   \hline
   0.075
   \end{array}
   \]

   The difference in the estimated and actual amounts is 0.075 grams.

   c. How many grams are in one dose of medicine? Explain your strategy for solving this problem.

   \[
   \begin{array}{c}
   5.985 \\
   2.925 \\
   \hline
   2.06 \\
   - 0.5 \\
   \hline
   0.25
   \end{array}
   \]

   I used the algorithm to find my answer.

   There are 5.985 grams of medicine in one dose.

   d. Round the weight of one dose to the nearest gram.

   \[
   5.985 g \approx 6 g
   \]